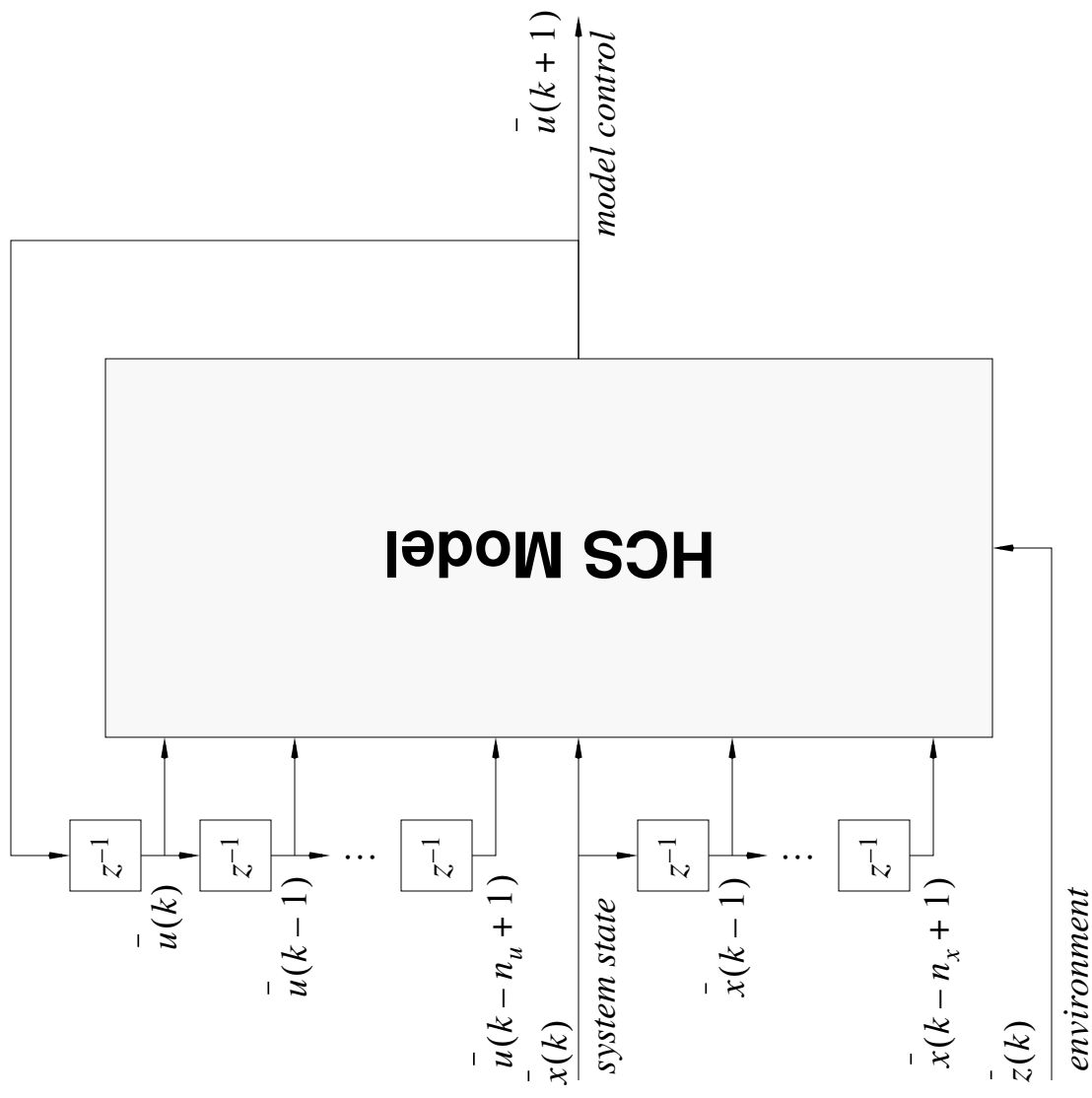
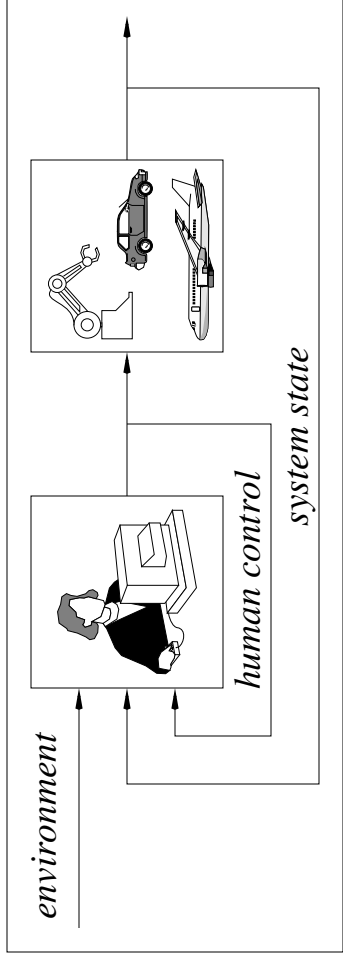
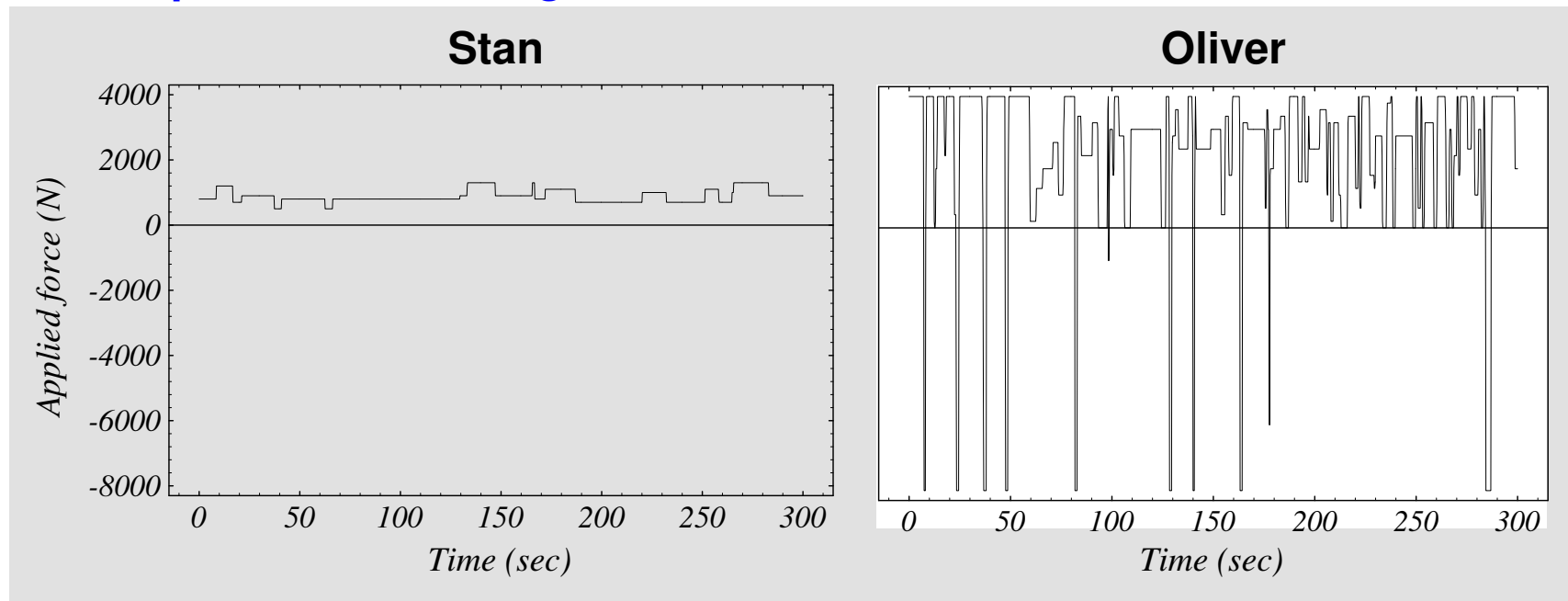


# Learning human control strategies



# Human control strategy

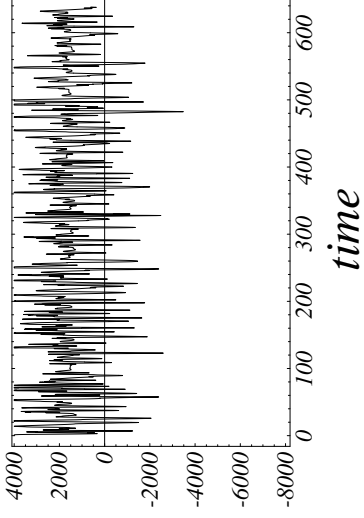
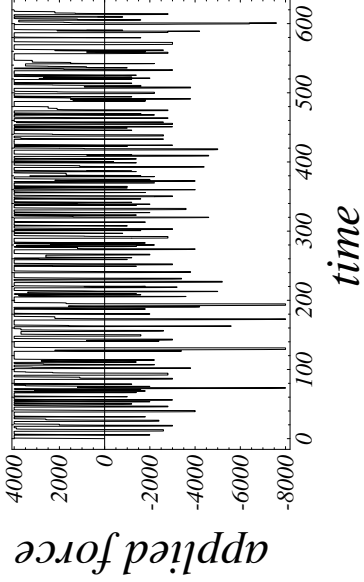
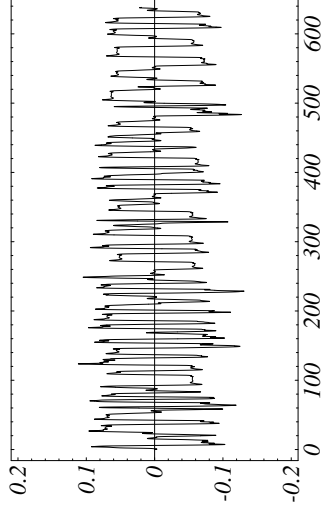
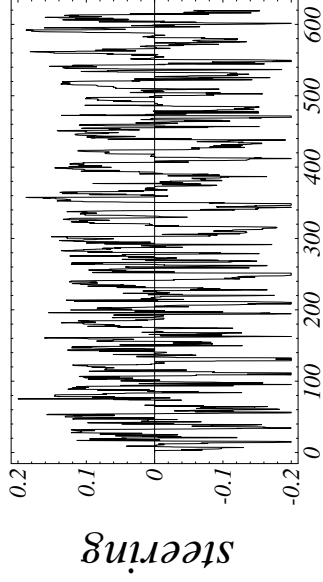
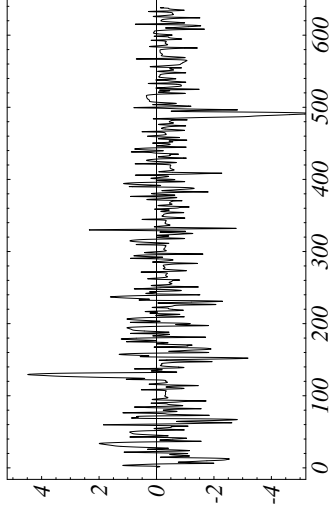
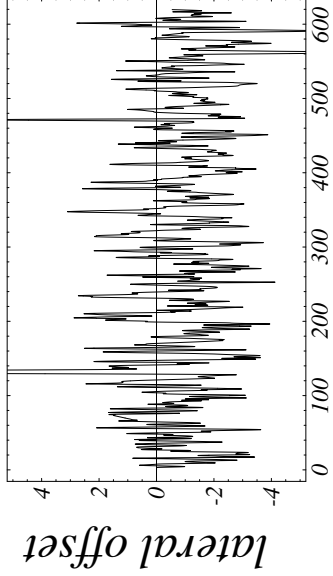
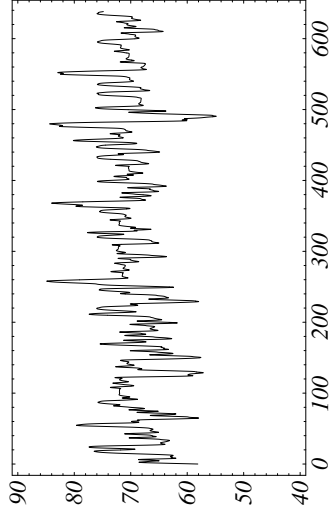
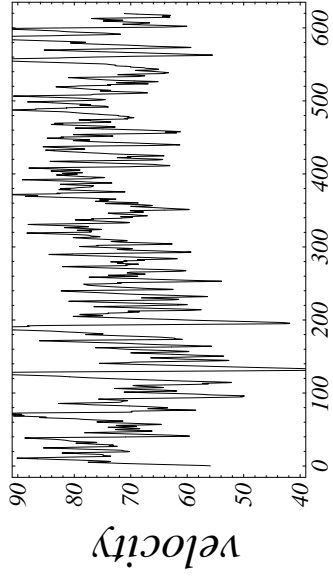
- **Dynamic, reaction skill**, with reasonably well-defined I/O representation
  - *Control gains*
  - *Control structure/approach*
  - *Interaction with environment/surrounding*
- **No abstract or high-level reasoning**
- **Example: human driving**



# Learning human control strategy

- **Difficult to model human control strategy *analytically*.**
- **Unknown individual controller properties**
  - *Structure*
  - *Order*
- **Human control strategy modeling complications**
  - *Dynamic*
  - *Stochastic — errors and inconsistencies*
  - *Possibly discontinuous*
  - *Possibly nonlinear*
- **Continuous learning approach: neural networks**

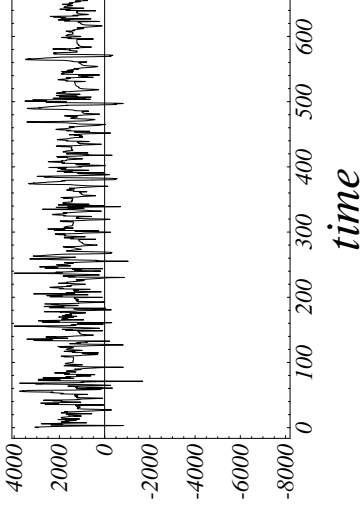
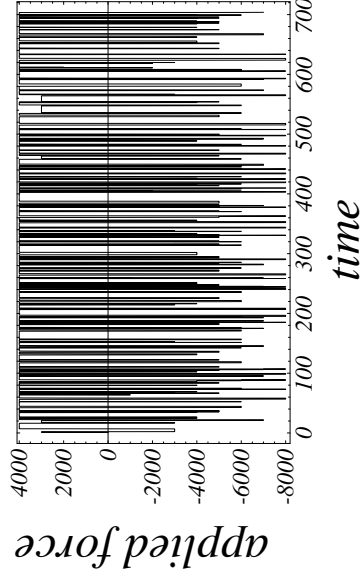
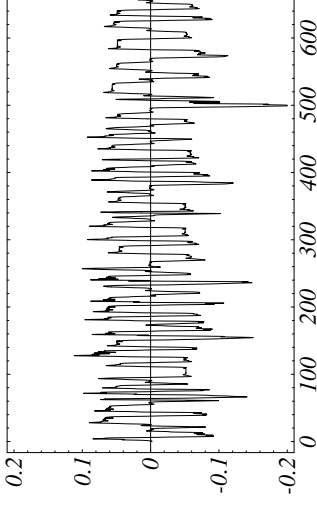
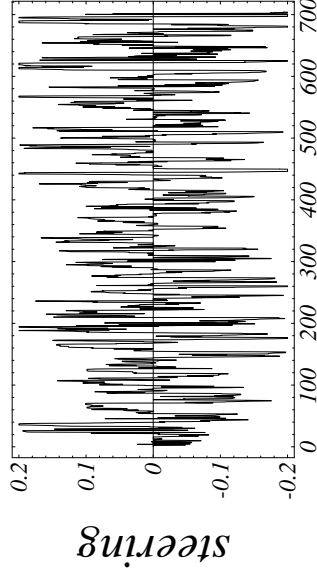
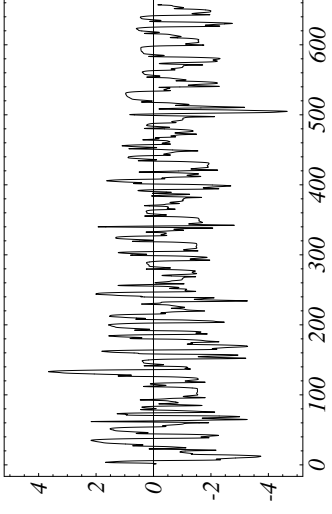
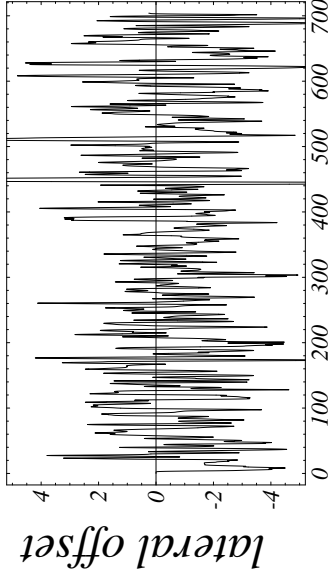
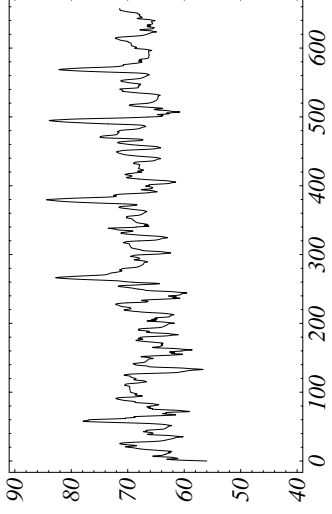
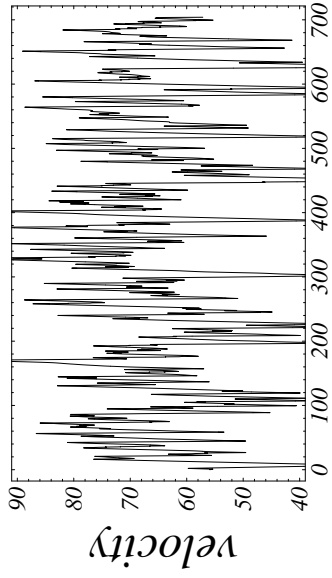
# HCS model example: Ck



*Groucho's control*

*Ck model control*

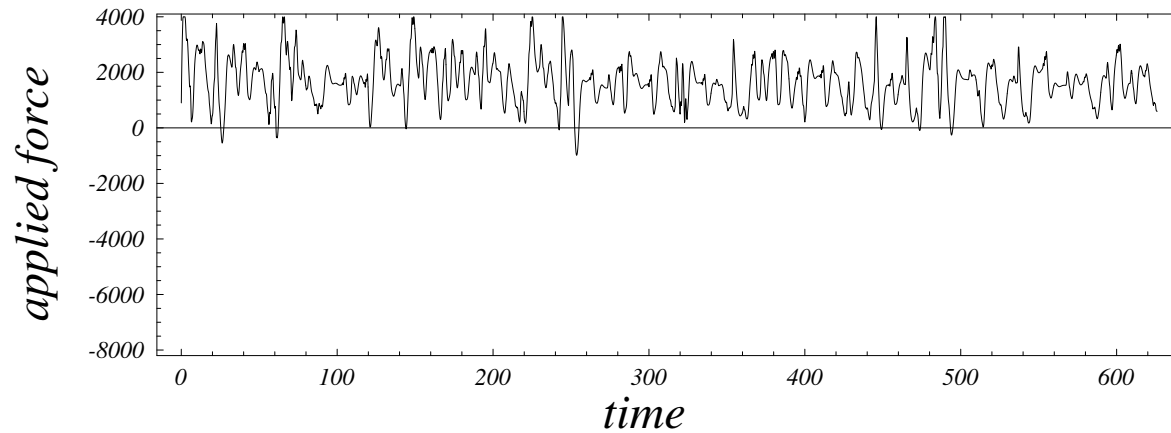
# HCS model example #2: Ck



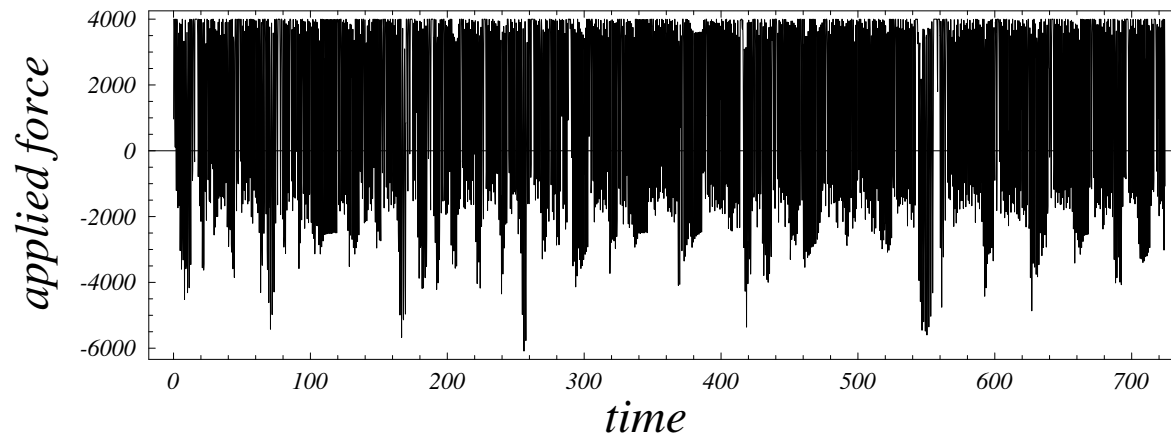
*Harpo's control*

*Ck model control*

## Additional hidden units in *neural network*



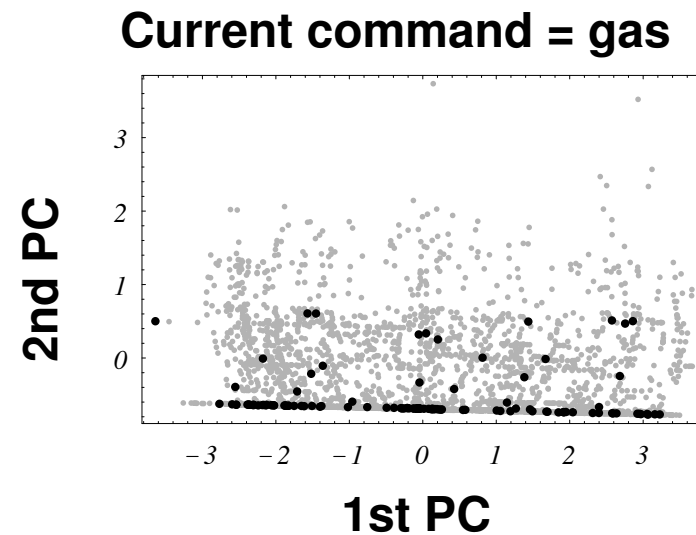
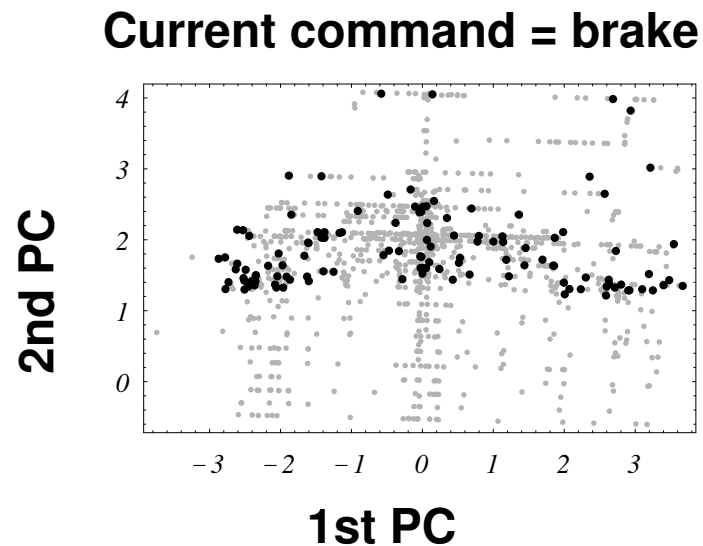
**linear model**



**one additional  
hidden unit**

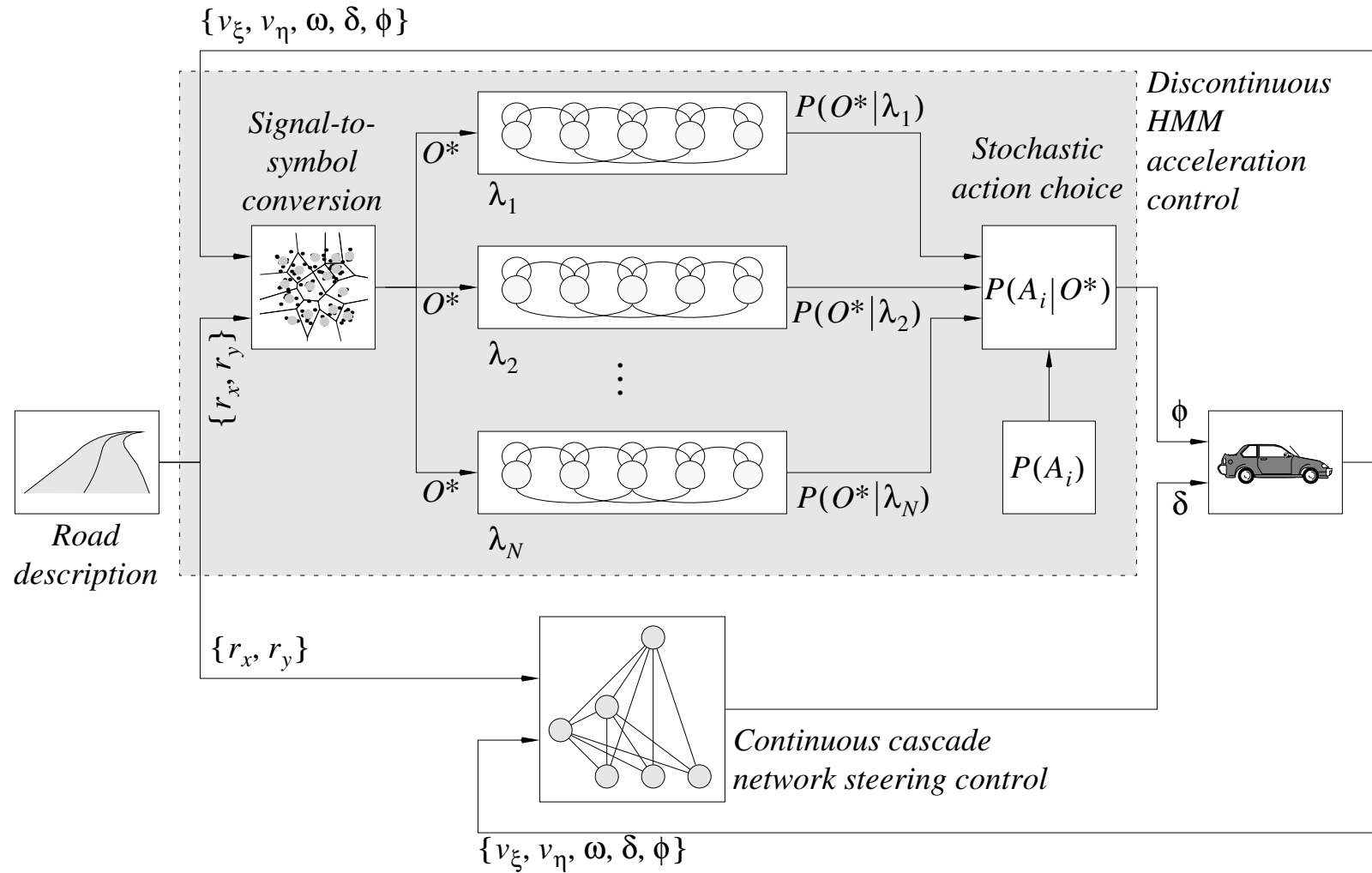
## Need for discontinuous learning

- $Cq$ ,  $Ck$  models are convergent (stable) strategies, but are not “similar.”
- In reduced dimensional plot, “switches” overlap “nonswitches.”



- Continuous neural network may have difficulty modeling discontinuous (e.g. switching) control strategies.

# Hybrid continuous/discontinuous control





# Actions

- **Applied force  $> 0$  (gas is currently active):**
  - $A_1$  : *do nothing.*
  - $A_2$  : *increase applied force.*
  - $A_3$  : *decrease applied force, but keep  $> 0$ .*
  - $A_4$  : *switch to braking*
- **Applied force  $< 0$  (brake is currently active):**
  - $A_5$  : *do nothing*
  - $A_6$  : *increase braking force*
  - $A_7$  : *decrease braking force*
  - $A_8$  : *switch to accelerator*

## Statistical model and priors

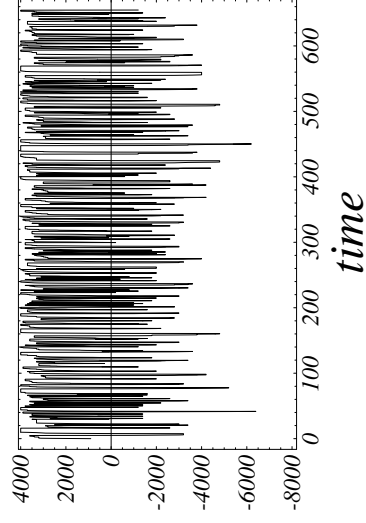
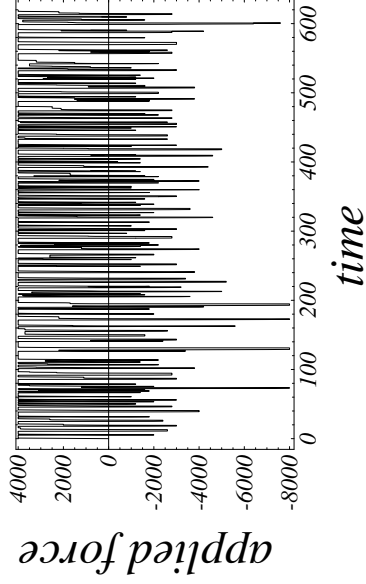
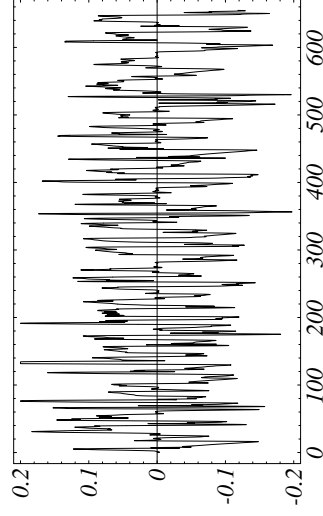
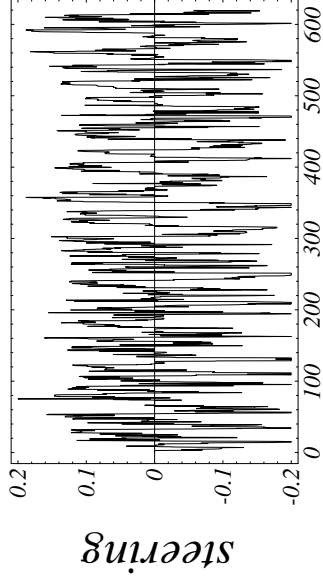
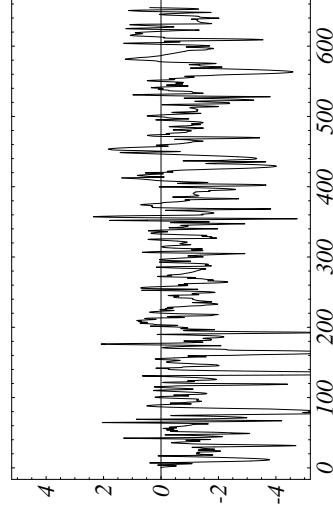
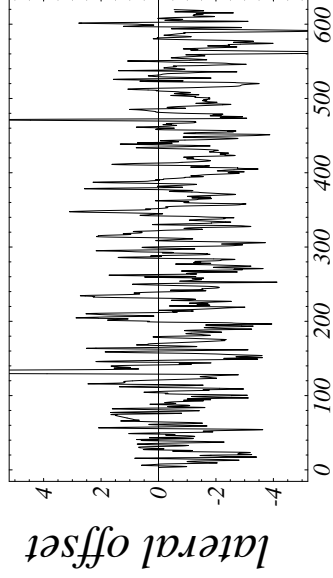
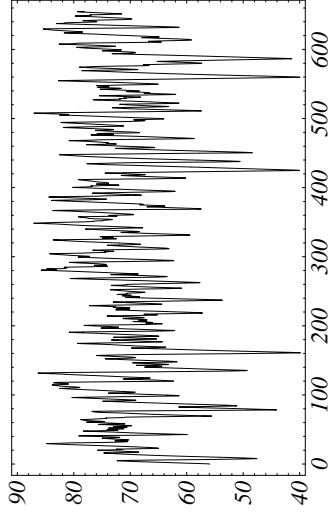
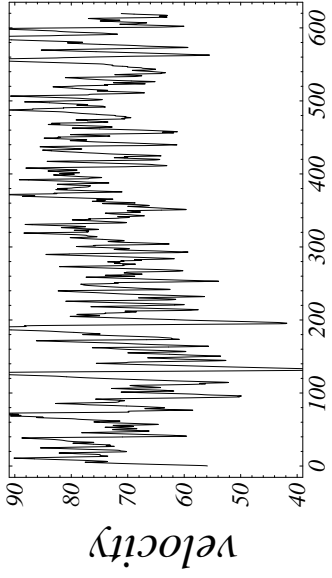
- **Single-state HMMs (encode arbitrary statistical distribution of inputs).**

$$P(O^*|A_i) \equiv P(O^*|\lambda_i)$$

- **Priors: frequency of occurrence for action  $A_i$  in human data set**

$$P(A_i|O^*) \propto P(O^*|\lambda_i)P(A_i)$$

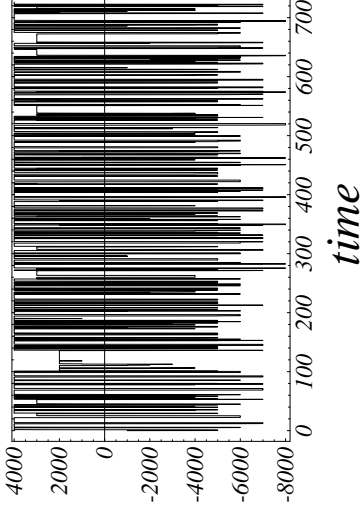
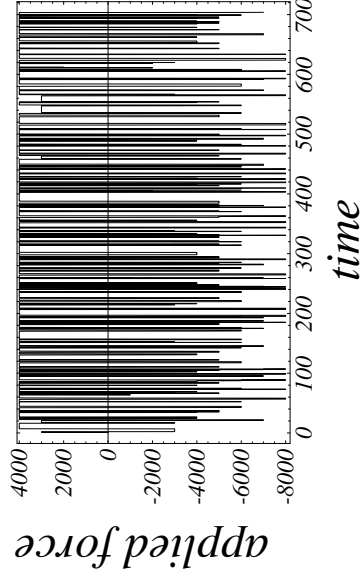
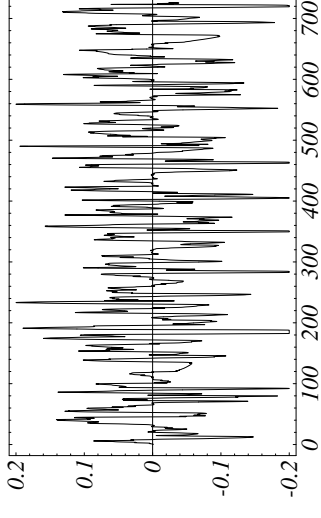
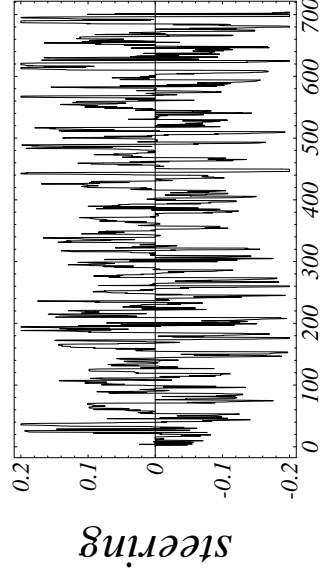
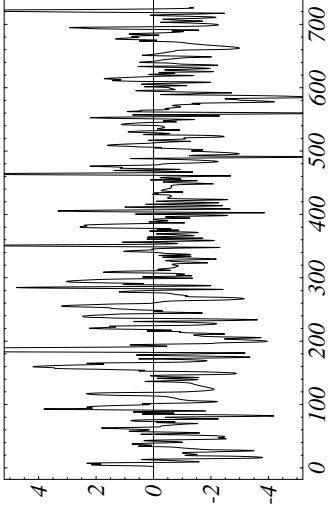
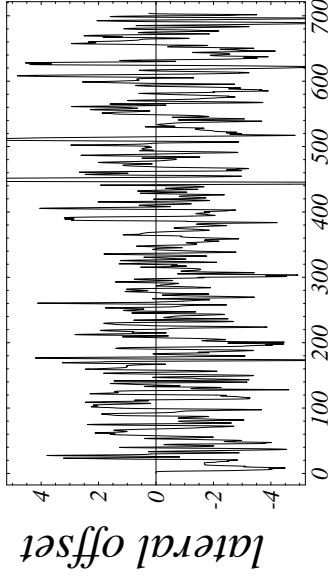
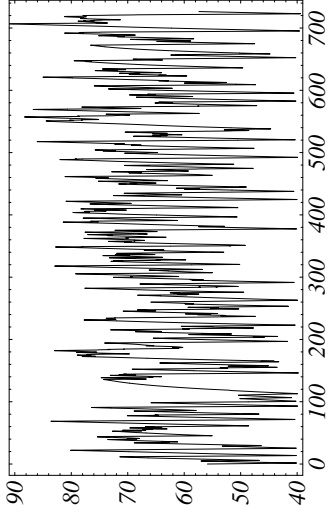
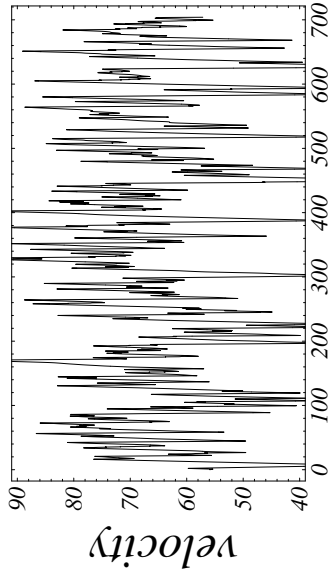
# HCS model example: hybrid



*Groucho's control*

*hybrid model control*

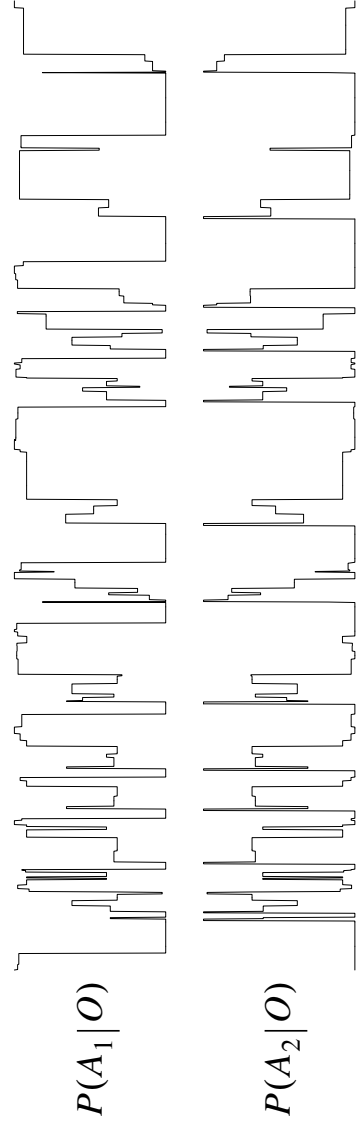
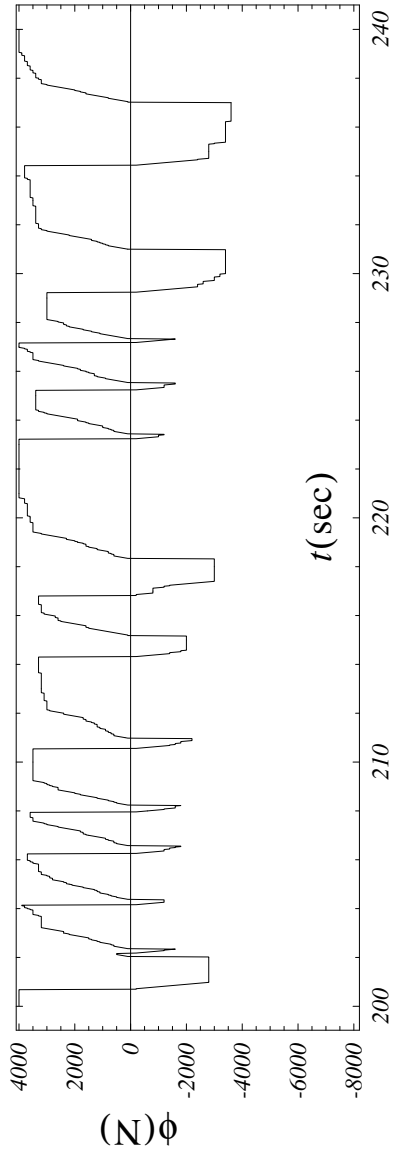
# HCS model example #2: hybrid



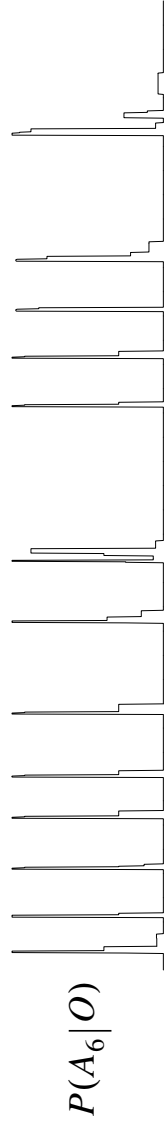
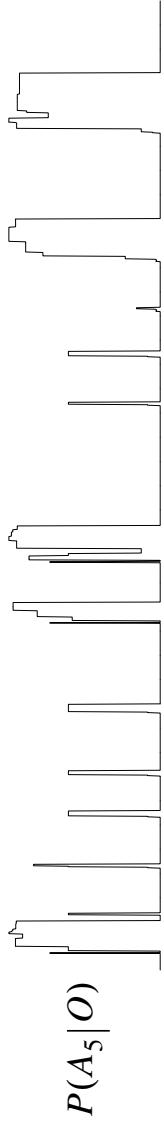
*Harpo's control*

*hybrid model control*

# A closer look



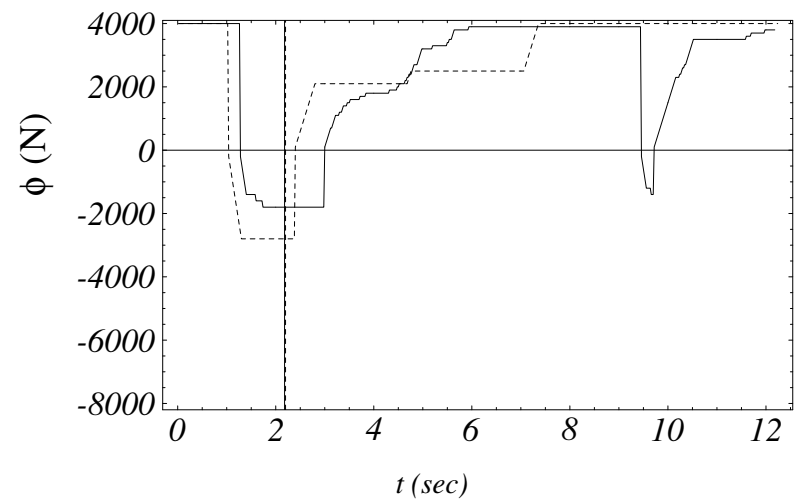
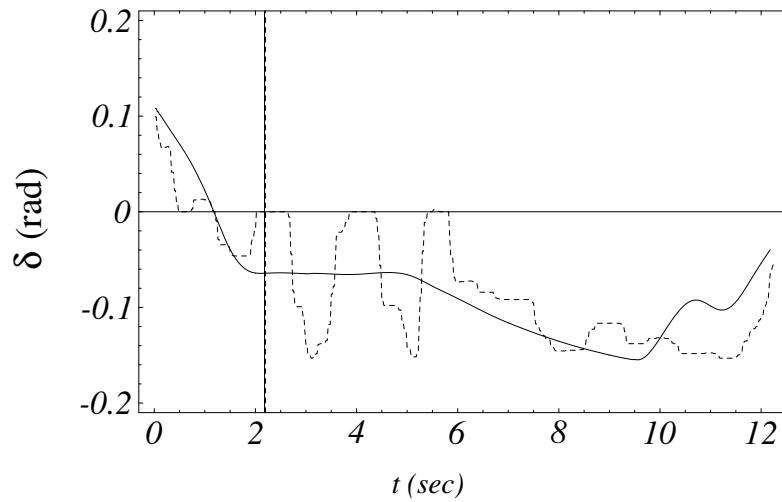
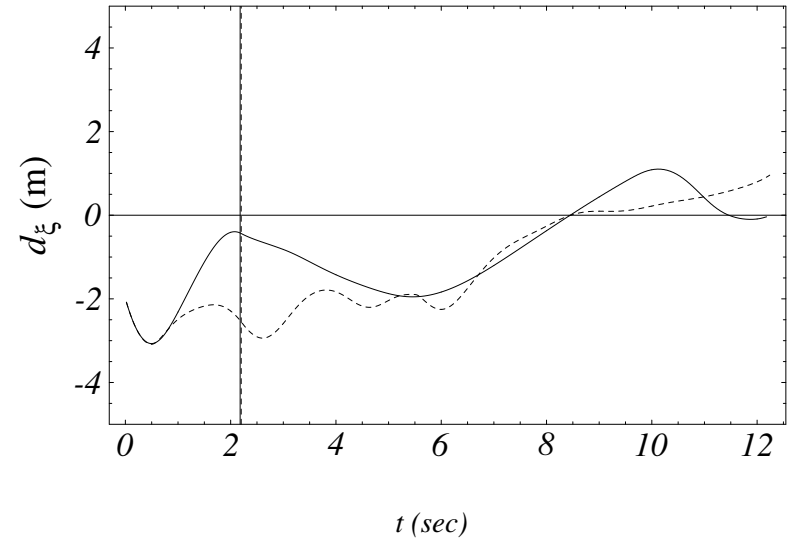
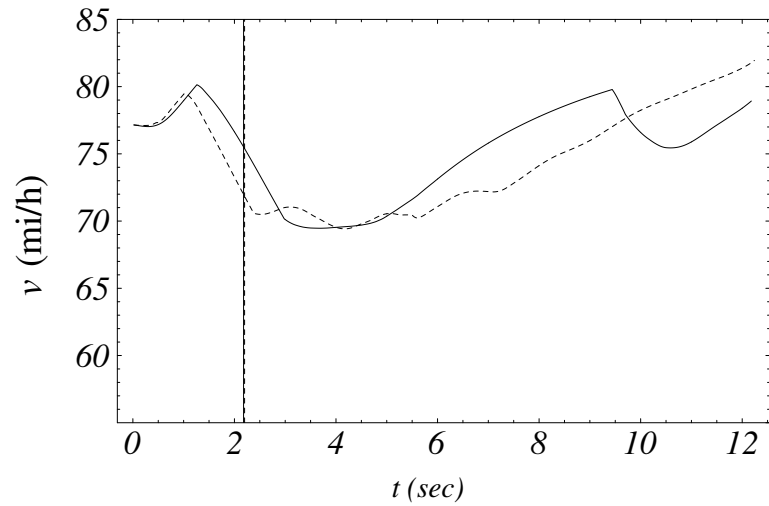
$P(A_4|O)$  *switch (gas to brake)*



$P(A_8|O)$  *switch (brake to gas)*

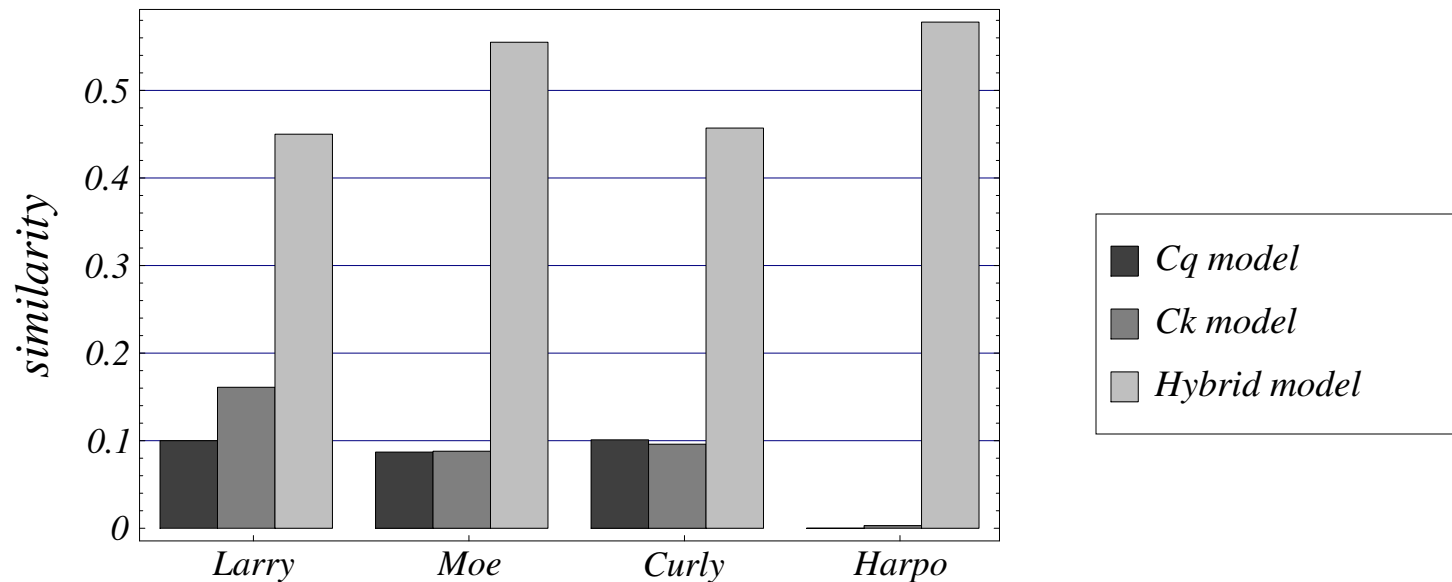


# Sample Groucho turning maneuver



# Human-to-model validation

- Quantify qualitative observations



- Hybrid model exhibits greater similarity than either of the purely NN-based modeling approaches.

# Model-to-human classification

**Table 1: Hybrid model-to-human matching**

$\sigma$	<i>Larry</i>	<i>Moe</i>	<i>Groucho</i>	<i>Harpo</i>
<i>Larry's model</i>	<b>0.450</b>	0.329	0.315	0.069
<i>Moe's model</i>	0.126	<b>0.555</b>	0.338	0.217
<i>Groucho's model</i>	0.152	0.377	<b>0.457</b>	0.206
<i>Harpo's model</i>	0.013	0.134	0.127	<b>0.578</b>

**Table 2: *Ck* model-to-human matching**

$\sigma$	<i>Larry</i>	<i>Moe</i>	<i>Groucho</i>	<i>Harpo</i>
<i>Larry's model</i>	0.161	<b>0.166</b>	0.118	0.157
<i>Moe's model</i>	0.056	<b>0.088</b>	0.063	0.041
<i>Groucho's model</i>	0.056	0.066	<b>0.096</b>	0.040
<i>Harpo's model</i>	0.006	0.008	<b>0.012</b>	0.003