

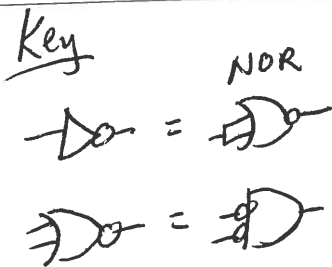
Open book and open notes, 90-minute examination. No electronic devices are permitted.

Page 1)	9 points	<u>Lucas</u>	Page 2)	23 points	<u>2 Daniel / 3 Aaron</u>
Page 3)	18 points	<u>4 Caleb / 5 Alan</u>	Page 4)	17 points	<u>6-8 Veronica / 9 Kyle</u>
Page 5)	18 points	<u>10 Wyatt / 11 Casey</u>	Page 6)	15 points	<u>12 Cody</u>
TOTAL		_____	of 100		<i>Kevin - total points</i>

Re-grade requests must be handed in the day exams are returned in class. Write the problem number you wish reviewed. A maximum of three review problems is allowed. Do not write anywhere else on the exam other than below or you will receive a zero on the exam.

1. Directly synthesize a circuit for the following equation using only 2 Input NOR gates only. (9 pt.)

$Y = \overline{A * (B * C)} + E + \overline{D}$; A.L, B.H, C.L, D.H, E.L, Y.H Do Not Simplify the Equation!



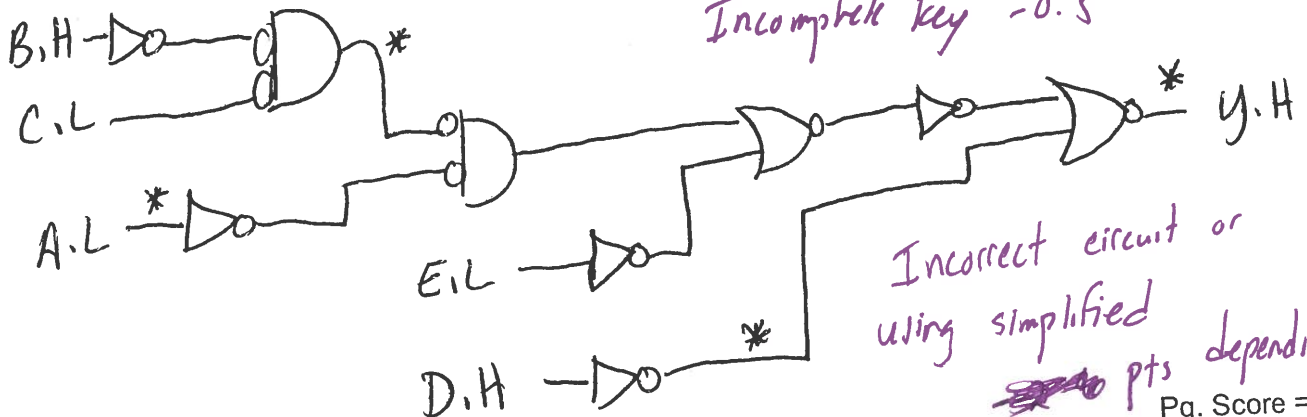
MOST OPTIMAL solution = Full credit

Each gate = 1pt.

*Any # of gates over 9 AND CORRECT
 -0.5 pt per gate*

No key - 2 pt

Incomplete key - 0.5



*Incorrect circuit or using simplified
 -7-9 pts depending*

Pg. Score =

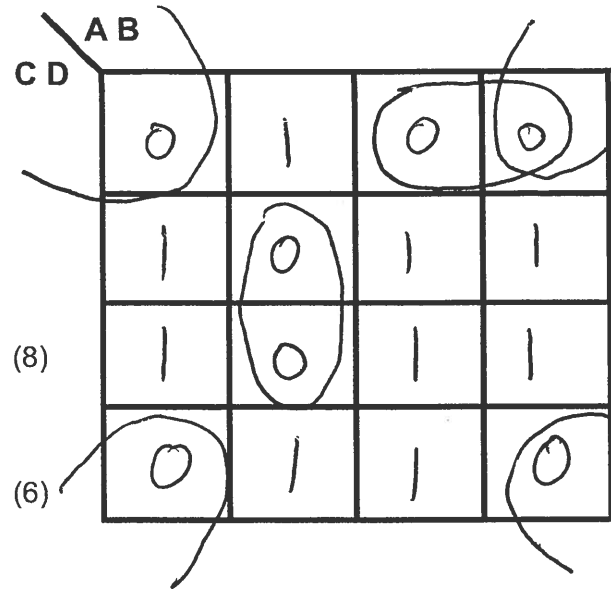
2. Find the **minimum sum of products** and **minimum product of sums** for the logic equation below using a K-Map. (14 pt.)

$$Y = (A+B+C+D)(\bar{A}+\bar{B}+C+D)(\bar{A}+C+D)(B+\bar{C}+D)(A+\bar{B}+\bar{D})$$

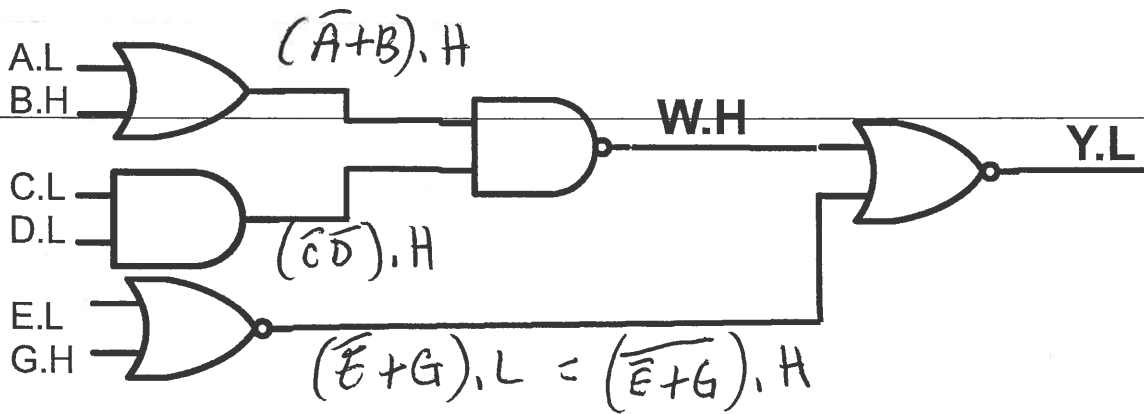
$$Y \text{ (MSOP)} = \frac{\bar{A}\bar{B}\bar{D} + \bar{B}\bar{D} + AD + \uparrow}{2 \quad 2 \quad 2 \quad 2} \quad (8)$$

$$Y \text{ (MPOS)} = \frac{(B+D)(A+\bar{B}+\bar{D})(\bar{A}+C+D)}{2 \quad 2 \quad 2} \quad (6)$$

ABC
or
BCD



3. Derive the logic equations for the following signals listed after the circuit below. **Show all intermediate signals as HIGH true for partial credit purposes. DO NOT SIMPLIFY YOUR ANSWER!**



$$W.H = \frac{(\bar{A}+B)(\bar{C}\bar{D})}{2 \quad 2} \quad (5 \text{ pt.})$$

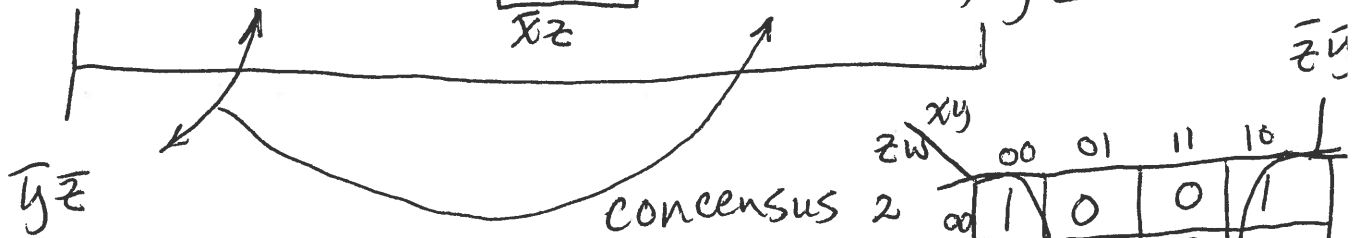
$$Y.L = \frac{(\bar{A}+B)(\bar{C}\bar{D}) + \overline{E+G}}{1 \quad 3} \quad (4 \text{ pt.})$$

4. Simplify the equation below with De Morgan's Rule and Boolean Identities to find the MSOP. (10 pt.)

$$Y = \overline{(X+Y+Z)} \overline{(X+Y+W)} \overline{(X+Z+W)} \overline{(X+Z)} \overline{(X+Z+W)} \overline{(X+Y+Z)}$$

$$\overline{X+Y+Z} + \overline{X+Y+W} + \overline{X+Z+W} + \overline{X+Z} + \overline{X+Z+W} + \overline{X+Y+Z}$$

$$\overline{X} \overline{Y} \overline{Z} + \overline{X} \overline{Y} \overline{W} + \overline{X} \overline{Z} \overline{W} + \overline{X} \overline{Z} + \overline{X} \overline{Z} \overline{W} + \overline{X} \overline{Y} \overline{Z}$$



$$Y = \overline{X} \overline{Z} + \overline{Y} \overline{Z} + \overline{X} \overline{Y} \overline{W}$$

xy \ zw	00	01	11	10
00	1	0	0	1
01	1	0	1	1
11	1	1	1	0
10	1	1	0	0

MSOP $\overline{X} \overline{Z}$ $\overline{X} \overline{Y} \overline{W}$

5. A student would like to design a multiplier that computes the product of a 2 bit unsigned number times a 3 bit unsigned number. i.e. $P = M1:0 \times N2:0$; where all numbers are unsigned binary

How many bits are required for P? 5 (2 pt.)

Write the Canonical Sum of Products (CSOP) for the most significant bit of P based on inputs M1:0 and N2:0 below. (8 pt.)

* $3 \times 7 = 21$

* $3 \times 6 = 18$

$3 \times 5 = 15$

$$P_4 = M_1 M_0 N_2 N_1 N_0 + M_1 M_0 N_2 N_1 \overline{N_0}$$

$P_4 = M_1 M_0 N_2 N_1$ - 1 simplified

-1/2 if not
Pn or Pans

-4 if 1 term is correct

6 – 8. Perform the following addition, subtraction and multiplication. (9 pt.)

$$\begin{array}{r} 1 \\ 10111 \\ 111001 \\ 101101 \\ + 111111 \\ \hline 10100101 \end{array}$$

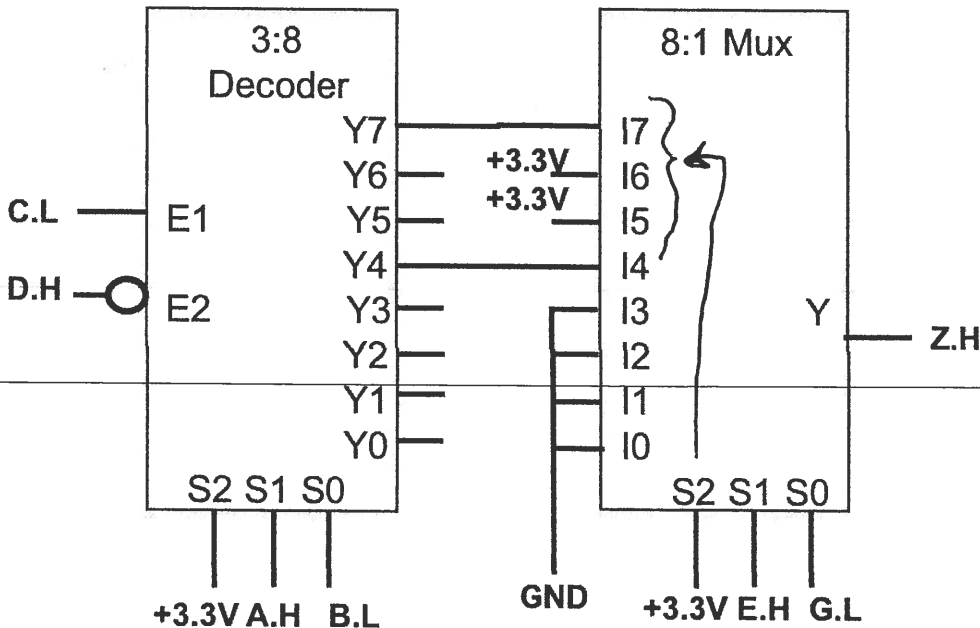
$$\begin{array}{r} 2 \\ 0110112 \\ 10010001 \\ - 01111110 \\ \hline 00010011 \end{array}$$

$$\begin{array}{r} 10101.01 \\ \times 101.01 \\ \hline \end{array}$$

$$\begin{array}{r} 10101.01 \\ 1010101.00 \\ 101.0101 \\ \hline 1101111.1001 \end{array}$$

3
[-1 wrong carry] 3
on any

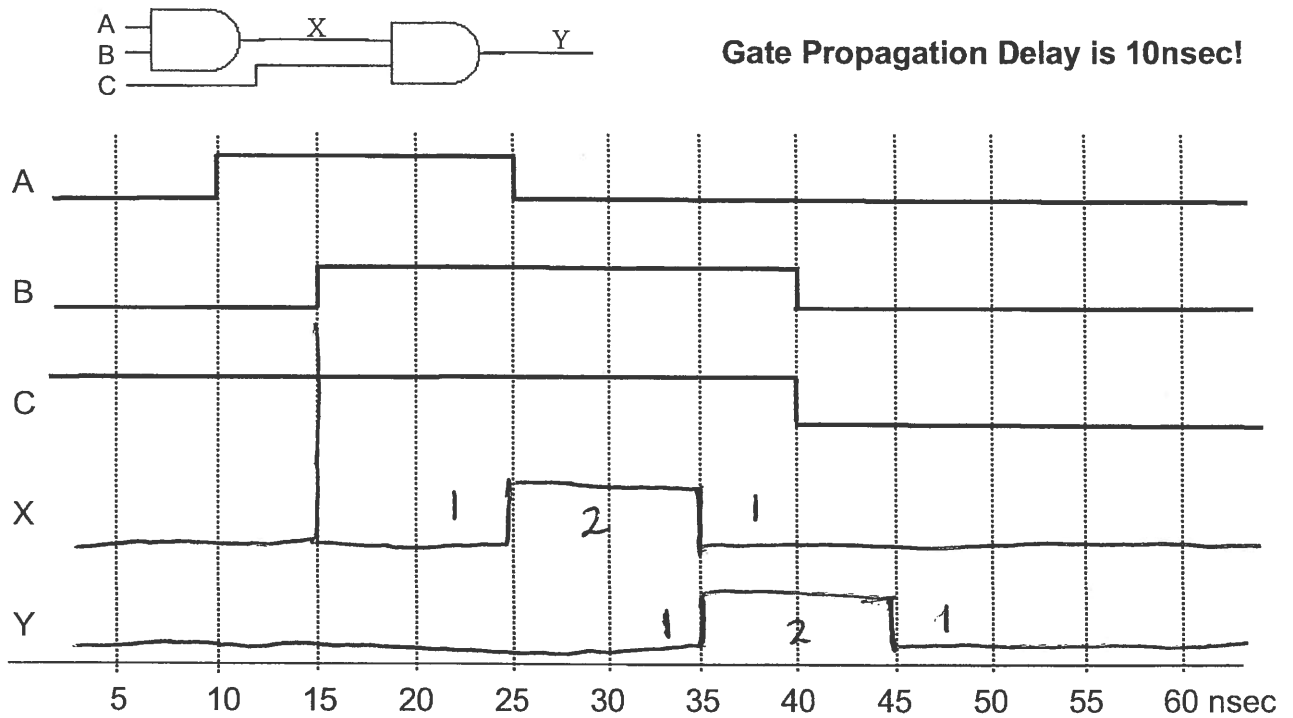
9. For the circuit below, derive the logic equation for Z.H. **Do not Simplify!** (8 pt.)



7	H	H	H	6
4	H	L	L	5
	H	H	H	7
	H	L	L	4

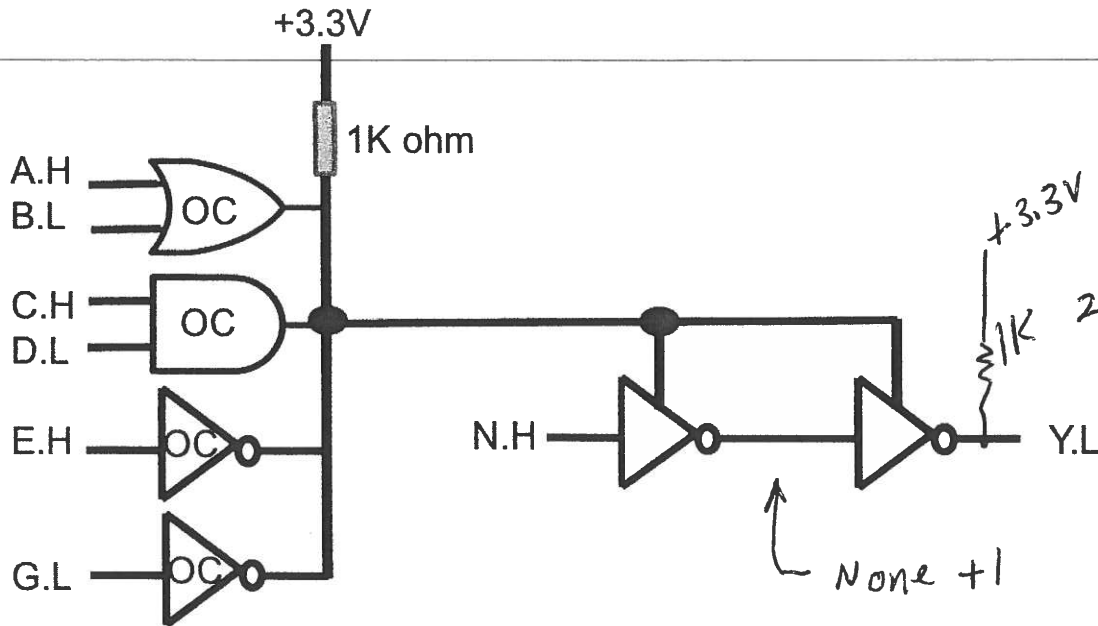
$$Z.H = \frac{EG + \bar{E}\bar{G} + \bar{C}\bar{D}A\bar{B}E\bar{G} + \bar{C}\bar{D}A\bar{B}E\bar{G}}{1 \quad 1 \quad 3 \quad 3}$$

10. Given the circuit below complete the voltage timing diagram for signals X and Y. Assume all devices have a **10nsec** propagation delay. (8 pt.) Assume **A=L, B=L, C=H** initially. **Gate Propagation Delay is 10nsec!**



+1 if size of pulse is correct (out of 2)

11. For the circuit below derive the **logic equation for Y** and **add the required missing Pull-up or Pull-down resistor** to make Y a function of A,B,C,D, E, G and N. (10 pt.)



Y.L = $(A+B)(C\bar{D})(\bar{E})(G)(\bar{N})$

2 2 1 1 1

12. Create a device that decrements a **4 bit Signed Number** by 1. **N3:0** is the **signed input** and **M3:0** is the **signed output** equivalent to **N3:0 - 1**. For example, if a "3" is input to the device, the output should be "2". One additional output, **V**, should also be generated that indicates when an overflow occurs. For example, if decrementing an input by 1 creates an overflow condition, output **V = 1**, otherwise **V = 0**.

Draw the truth table for the device below:

N3	N2	N1	N0	M3	M2	M1	M0	V
0	0	0	0	1	1	1	1	0
1	0	0	1	0	0	0	0	0
2	0	1	0	0	0	0	1	0
3	0	1	1	0	0	1	0	0
4	1	0	0	0	0	1	1	0
5	1	0	1	0	1	0	0	0
6	1	1	0	0	1	0	1	0
7	1	1	1	0	1	1	0	0
-8	1	0	0	X	X	X	X	1
-7	1	0	1	1	0	0	0	0
-6	1	1	0	1	0	0	1	0
-5	1	1	1	1	0	1	0	0
-4	1	1	0	1	0	1	1	0
-3	1	1	0	1	1	0	0	0
-2	1	1	1	1	1	0	1	0
-1	1	1	1	1	1	1	0	0

(10 pt.) \rightarrow 2 for V column

Handwritten annotations: } 2 M & N (next to rows 0-3), } 2 (next to rows 4-7), } 2 (next to rows -8 to -5), } 2 (next to rows -4 to -1).

Derive the MSOP Logic Equation for **M0** and **V** (5 pt.):

$$M_0 = \overline{N_0}$$

2

$$V = N_3 \overline{N_2} \overline{N_1} \overline{N_0}$$

3