

Denavit-Hartenberg parameters

1. Summary of the link parameters in terms of the link frames [1]

$$a_i = \text{the distance from } \hat{Z}_i \text{ to } \hat{Z}_{i+1} \text{ measured along } \hat{X}_i. \quad (1)$$

$$\alpha_i = \text{the angle between } \hat{Z}_i \text{ and } \hat{Z}_{i+1} \text{ measured about } \hat{X}_i. \quad (2)$$

$$d_i = \text{the distance from } \hat{X}_{i-1} \text{ to } \hat{X}_i \text{ measured along } \hat{Z}_i. \quad (3)$$

$$\theta_i = \text{the angle between } \hat{X}_{i-1} \text{ and } \hat{X}_i \text{ measured about } \hat{Z}_i. \quad (4)$$

2. Summary of link frame attachment procedure [1]

1. Identify the joint axes and imagine (or draw) infinite lines along them. For steps 2 through 5 below, consider two of these neighboring lines (at axes i and $i + 1$).
2. Identify the common perpendicular between them, or point of intersection. At the point of intersection, or at the point where the common perpendicular meets the i th axis, assign the link frame origin.
3. Assign the \hat{Z}_i axis pointing along the i th joint axis.
4. Assign the \hat{X}_i axis pointing along the common perpendicular, or if the axes intersect, assign \hat{X}_i to be normal to the plane containing the two axes.
5. Assign the \hat{Y}_i axis to complete a right-hand coordinate system.
6. Assign $\{0\}$ to match $\{1\}$ when the first joint variable is zero. For $\{N\}$, choose an origin location and \hat{X}_N direction freely, but generally so as to cause as many linkage parameters as possible to become zero.

References

- [1] J. J. Craig, *Introduction to Robotics: Mechanics and Control, 2nd ed.*, Addison-Wesley, Reading, MA, 1989.